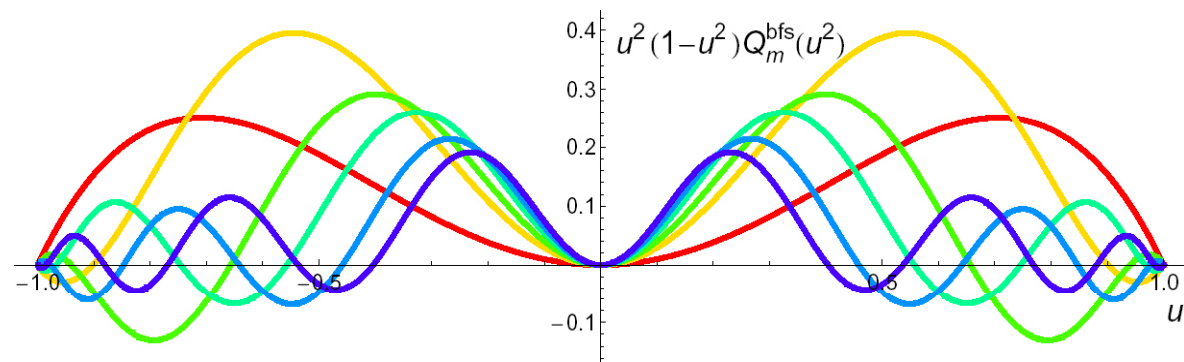
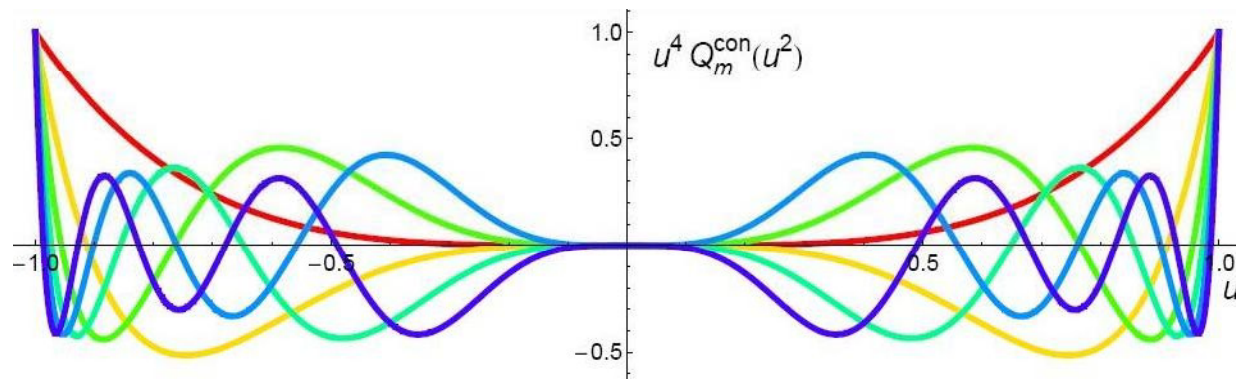


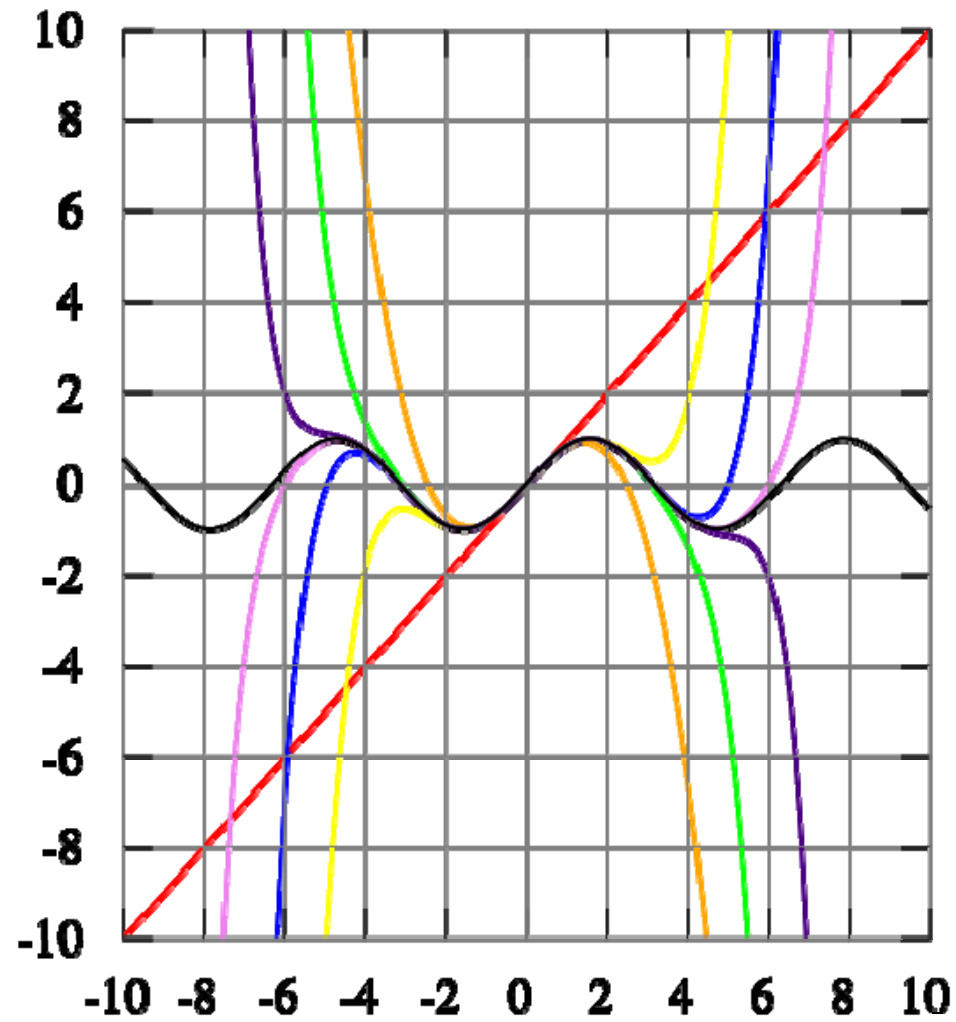
Introdução aos Polinómios Ortogonais



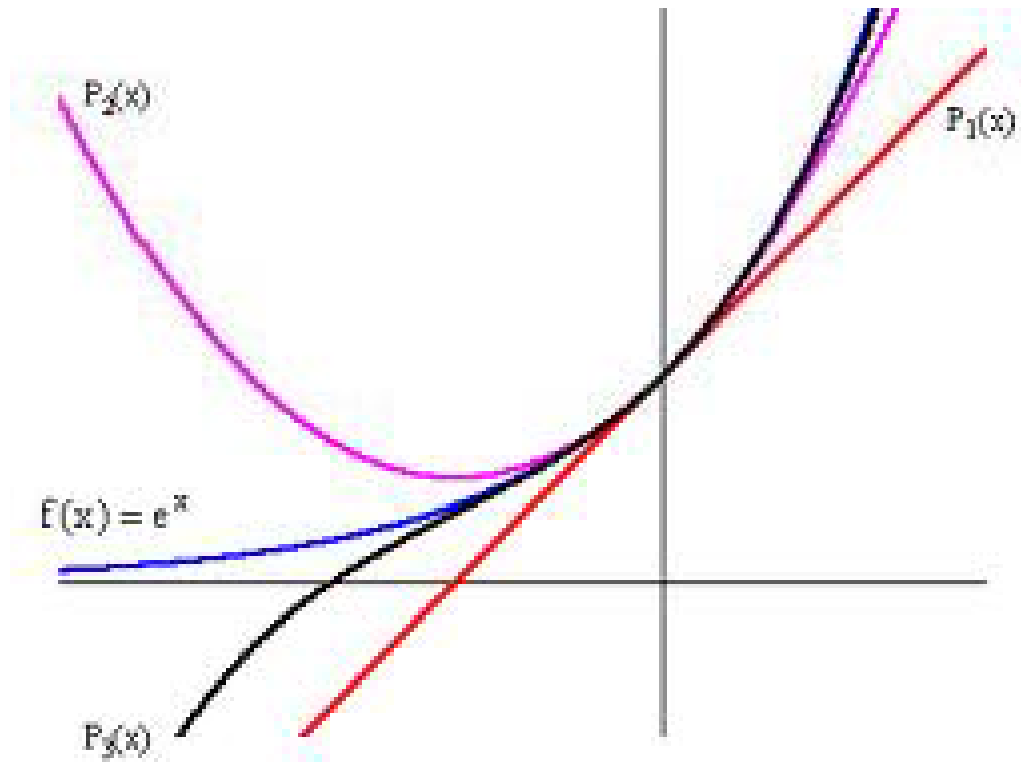
Índice de Conteúdos

- I. Aproximação com polinómios
- II. Compressão de Informação
- III. Regras de quadratura gaussiana
- IV. Interpretação eletrostática dos zeros
- V. Ótica (Polinomios de Zernike)
- VI. Átomo de hidrogénio (WWW)
- VII. Oscilador harmônico quântico (WWW)

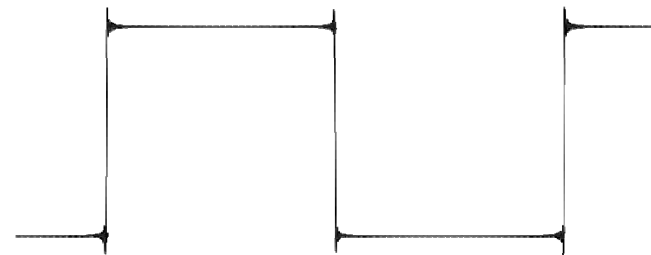
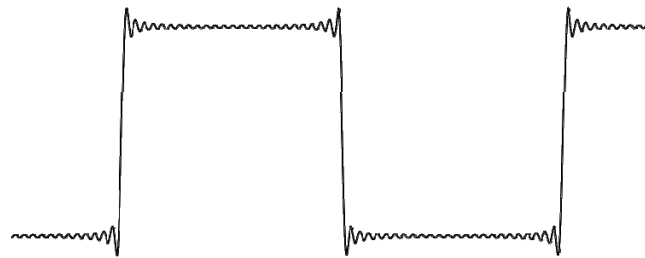
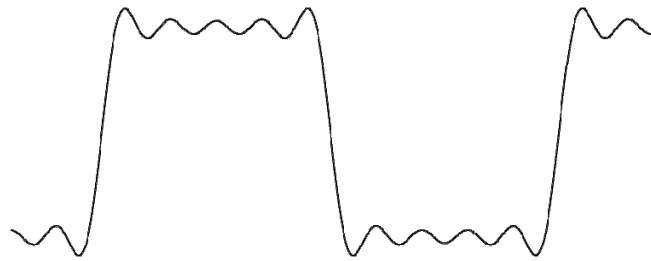
I. Aproximação com polinómios: Serie de Taylor



I. Aproximação com polinómios: Serie de Taylor



I. Aproximação com polinômios: Problema: fenômeno de Gibbs



II. Compressão de Informação Imagens

K.W. See et al. / Applied Mathematics and Computation 193 (2007) 346–359

		Original Image E													
<i>O</i>		2	4	6	8	10	12	14	16	18	20	22	24	26	28
<i>P</i>															
<i>P</i>		8.3	9.4	10.7	13.6	14.5	14.6	15.5	17.1	18.8	20.7	23.8	27.2	29.4	∞
DCT															
<i>P</i>															
<i>P</i>		8.7	8.9	9.6	10.9	13.6	14.6	14.8	15.0	16.1	19.9	21.8	24.2	34.7	38.7
Tchebichef															
<i>P</i>															
<i>P</i>		1.8	2.7	4.8	7.2	11.4	12.6	14.9	17.0	18.4	19.9	22.1	26.8	28.2	38.7
Krawtchouk															
<i>P</i>															
<i>P</i>		1.8	2.1	2.2	2.7	3.6	4.9	5.6	7.4	8.2	11.8	13.2	17.6	21.7	∞
Hahn															
<i>P</i>															
<i>P</i>		5.0	4.4	6.8	8.6	9.1	8.6	9.7	9.6	9.6	10.1	8.8	10.2	9.9	12.7
Poisson-Charlier															

Fig. 1. Image reconstruction of the letter "E" (grayscale 30×30) from orders 2 to 28, with the PSNR val

2.16

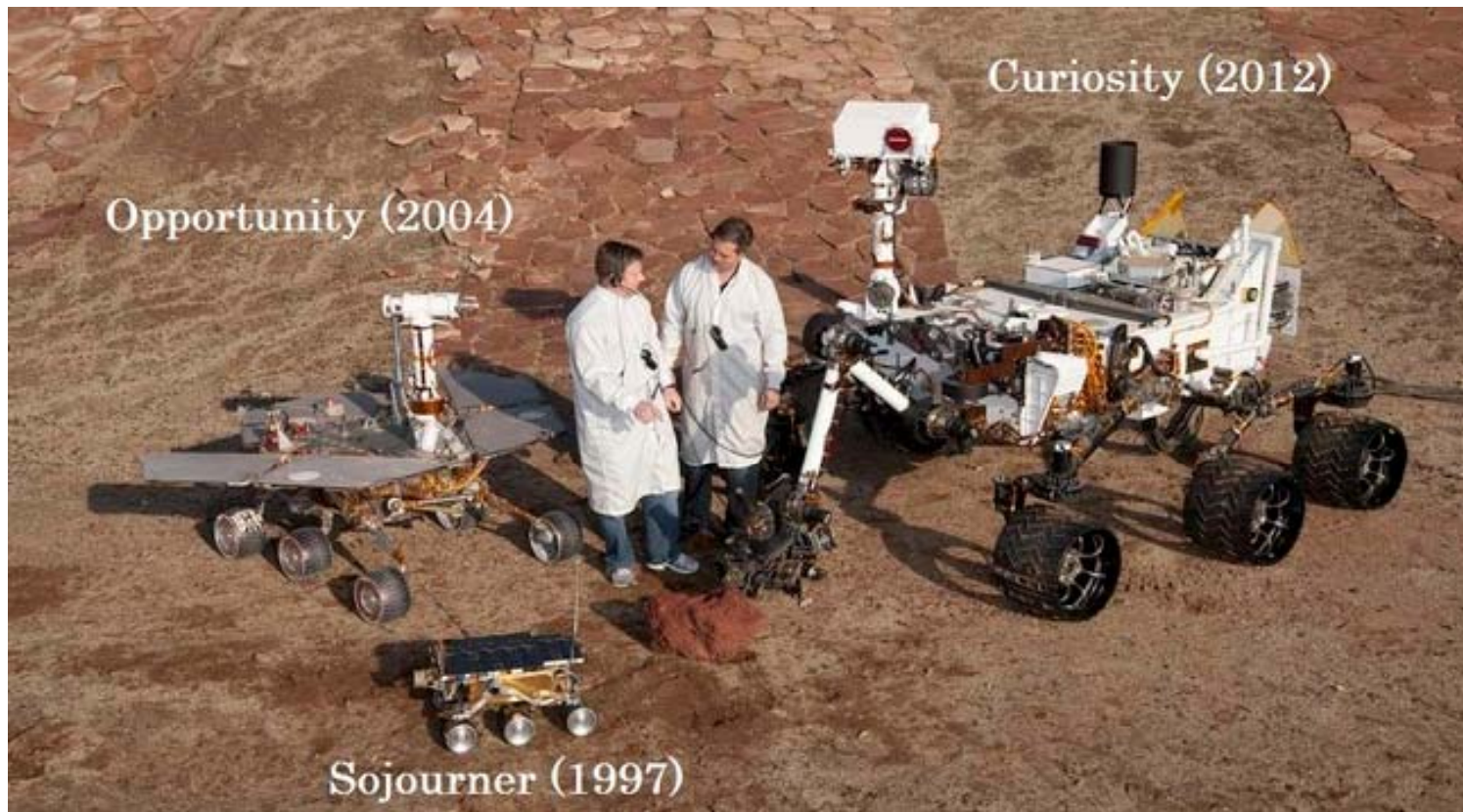
II. Compressão de Informação Imagens

K.W. See et al. / Applied Mathematics and Computation 193 (2007) 346–359

		Original Image									
<i>O</i>		10	15	20	25	30	35	40	45	50	55
		DCT									
<i>P</i>											
		20.0	22.0	23.3	25.1	26.8	28.4	30.5	32.6	34.8	37.5
		Tchebichef									
<i>P</i>											
		19.4	21.5	22.8	24.2	25.4	26.9	28.3	30.4	32.9	36.4
		Krawtchouk									
<i>P</i>											
		7.3	9.3	13.3	16.5	23.3	27.3	30.0	31.9	33.8	36.7
		Hahn									
<i>P</i>											
		5.4	6.0	7.1	7.9	9.6	10.9	12.8	14.7	18.1	21.5
		Poisson-Charlier									
<i>P</i>											
		8.4	8.4	8.4	8.7	9.0	9.4	9.4	9.4	9.6	9.7

5. Image reconstruction of the image Lena (grayscale 64×64) from orders 10 to 55, with the PSNR va

II. Compressão de Informação Telecomunicações



II. Compressão de Informação Telecomunicações

Pôr do sol em Marte (Spirit)
Credits: NASA/JPL



II. Compressão de Informação Telecomunicações



NASA Deep Space Network
(<http://deepspace.jpl.nasa.gov/dsn/>)

1. Goldstone, Estados Unidos (desierto de Mojave)
2. Canberra, Australia
3. Robledo de Chavela, Madrid (Espanha)

II. Compressão de Informação

Telecomunicações



US007249153B2

(12) **United States Patent**
Cheng et al.

(10) **Patent No.:** **US 7,249,153 B2**
(45) **Date of Patent:** **Jul. 24, 2007**

(54) **DATA COMPRESSION USING CHEBYSHEV
TRANSFORM**

6,051,027 A * 4/2000 Kapur et al. 703/5

(75) Inventors: **Andrew F. Cheng**, Potomac, MD (US);
S. Edward Hawkins, III, Ellicott City,
MD (US); **Lillian Nguyen**, Ellicott
City, MD (US); **Christopher A.**
Monaco, Silver Spring, MD (US);
Gordon G. Seagrave, Washington, DC
(US)

(73) Assignee: **The Johns Hopkins University**,
Baltimore, MD (US)

(*) Notice: Subject to any disclaimer, the term of this
patent is extended or adjusted under 35
U.S.C. 154(b) by 591 days.

OTHER PUBLICATIONS

Corr et al., "Discrete Chebyshev Transform A Matural Modification
of the DCT", 2000 IEEE, pp. 1142-1145.*

Anand R. Prasad; Audio Coding using Parametric Piecewise Mod-
eling; IEEE ICPWC '99; 1999; pp. 414-418; IEEE, New York, New
York.

Y. S. Zhu, S. W. Leung, Systolic Array Implementations for
Chebyshev Nonuniform Sampling; IEEE; 1992; pp. IV-177 to
IV-180; IEEE, New York, New York.

Gerard Leng; Compression of aircraft aerodynamic database using
multivariable Chebyshev polynomials; Advances in Engineering
Software 28 (1997); pp. 133-141; Elsevier Science Ltd.. Great
Britain.

II. Compressão de Informação

Telecomunicações

(22) Filed: **Aug. 1, 2003**

(65) **Prior Publication Data**
US 2004/0093364 A1 May 13, 2004

Related U.S. Application Data

(60) Provisional application No. 60/400,326, filed on Aug. 1, 2002.

(51) **Int. Cl.**
G06F 15/00 (2006.01)
G06F 17/14 (2006.01)

(52) **U.S. Cl.** **708/203**; 708/400

(58) **Field of Classification Search** 708/203,
708/400

See application file for complete search history.

(56) **References Cited**

U.S. PATENT DOCUMENTS

4,658,367 A * 4/1987 Potter 702/111

Primary Examiner—Chuong D. Ngo
(74) *Attorney, Agent, or Firm*—Francis A. Cooch

(57) **ABSTRACT**

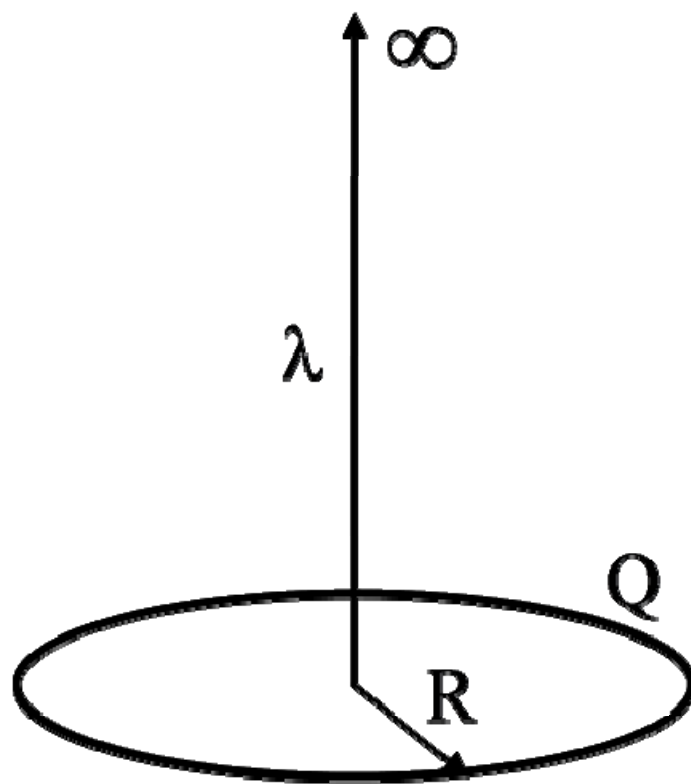
The present invention is a method, system, and computer program product for implementation of a capable, general purpose compression algorithm that can be engaged “on the fly”. This invention has particular practical application with time-series data, and more particularly, time-series data obtained from a spacecraft, or similar situations where cost, size and/or power limitations are prevalent, although it is not limited to such applications. It is also particularly applicable to the compression of serial data streams and works in one, two, or three dimensions. **The original input data is approximated by Chebyshev polynomials, achieving very high compression ratios on serial data streams with minimal loss of scientific information.**

27 Claims, 3 Drawing Sheets

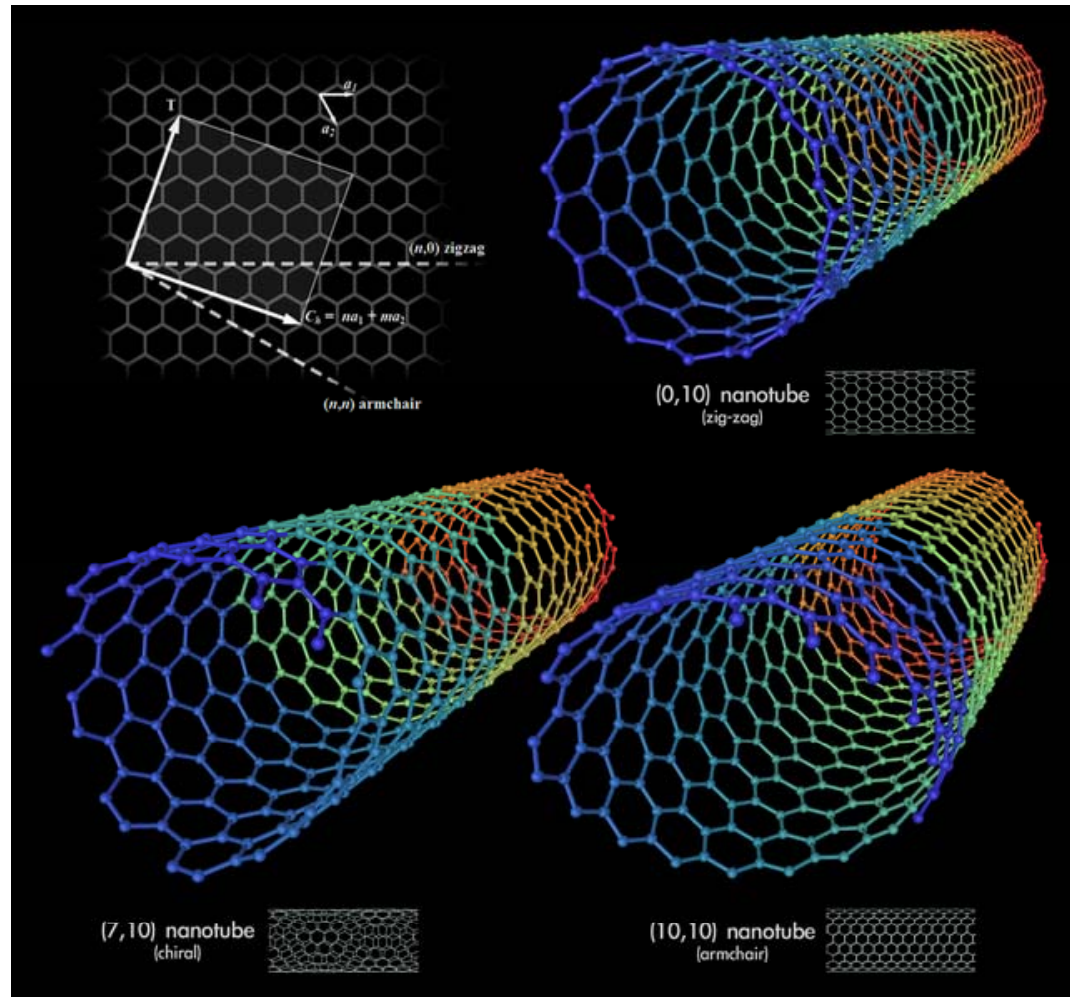
III. Regras de quadratura gaussiana

$$\int f(x)dx \approx \sum_{i=1}^n w_i f(x_i)$$

IV. Interpretação eletrostática dos zeros dos polinômios ortogonais



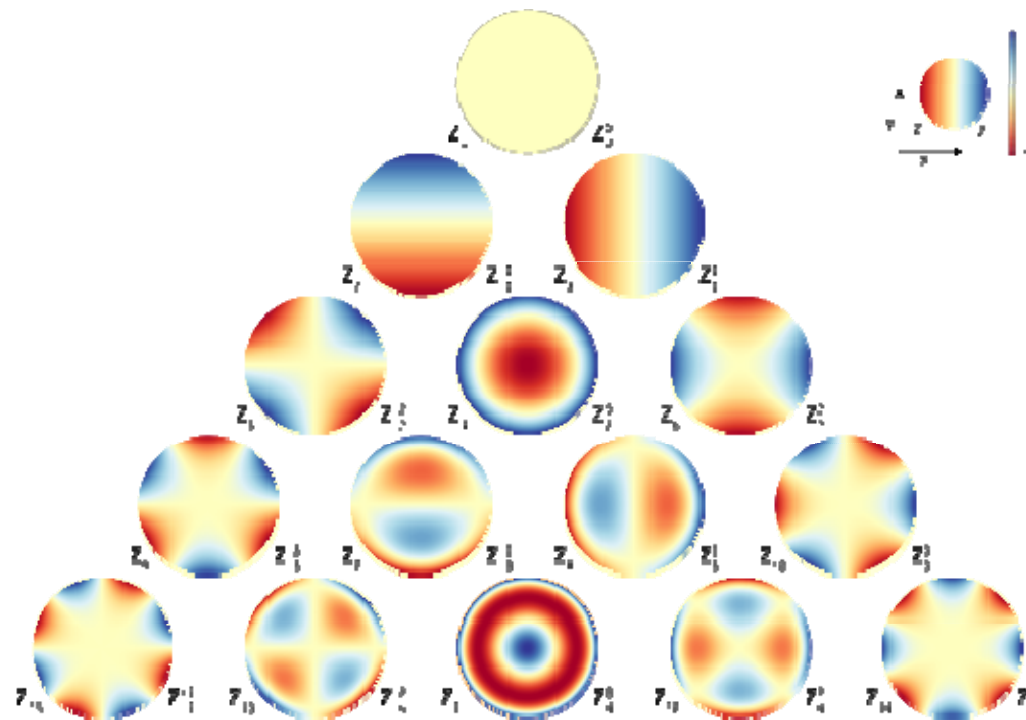
IV. Interpretação eletrostática dos zeros dos polinômios ortogonais -Carbon nanotubes



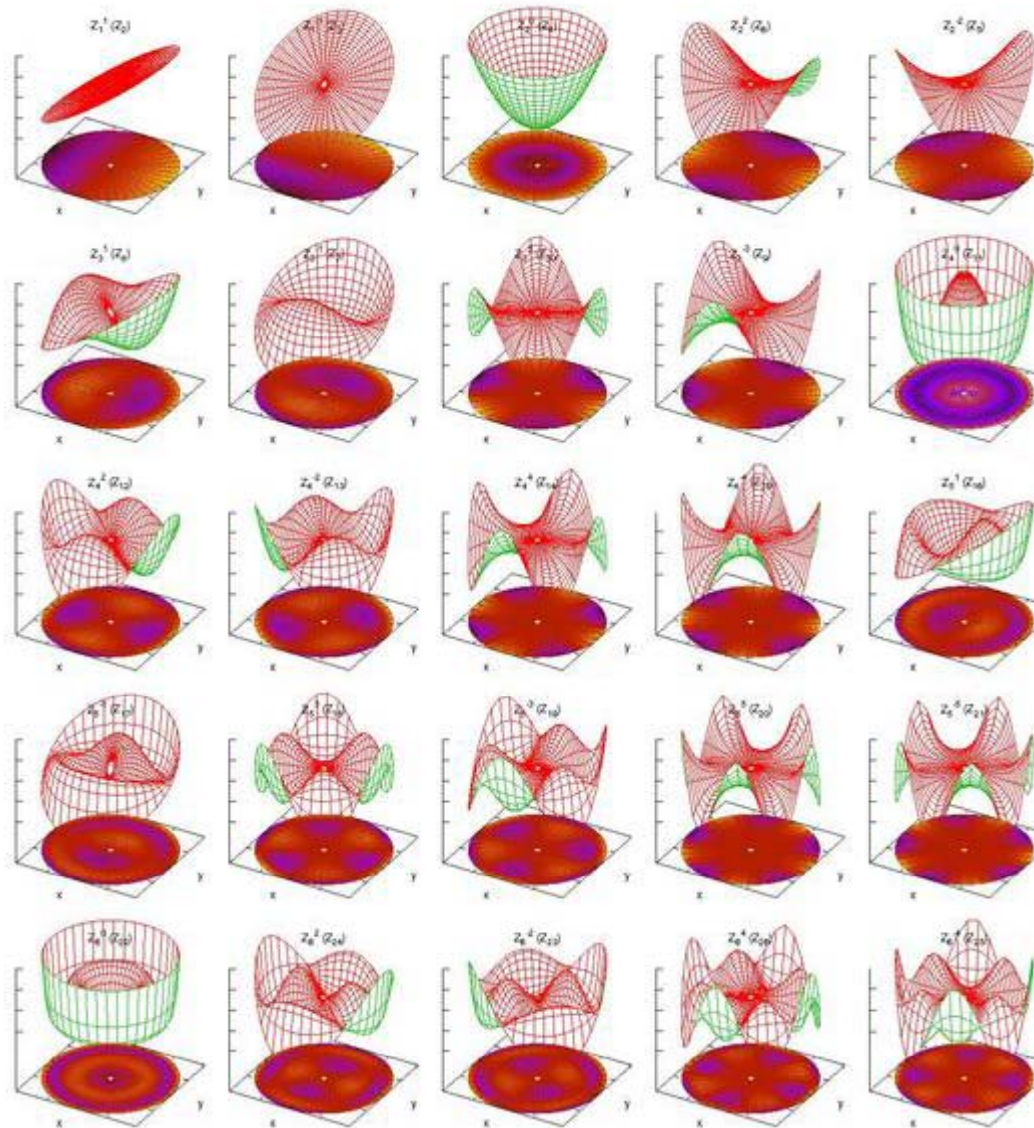
V. Ótica. Polinómios de Zernike

Applications of Zernike polynomials

The Zernike polynomials are a **basis** defined over the circular support area, typically the pupil planes in classical optical imaging at visible and infrared wavelengths through systems of lenses and mirrors of finite diameter.

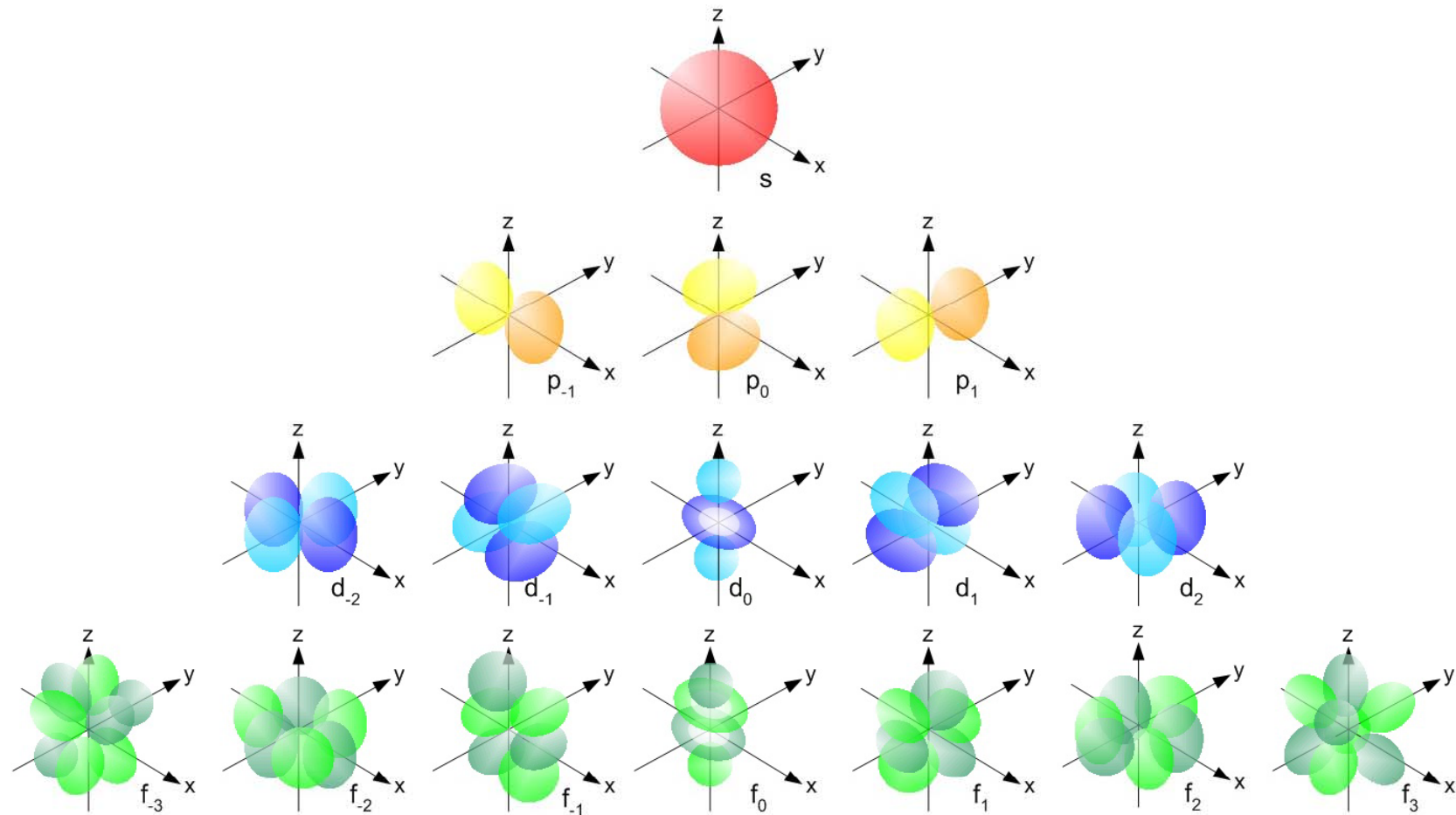


V. Ótica. Polinómios de Zernike



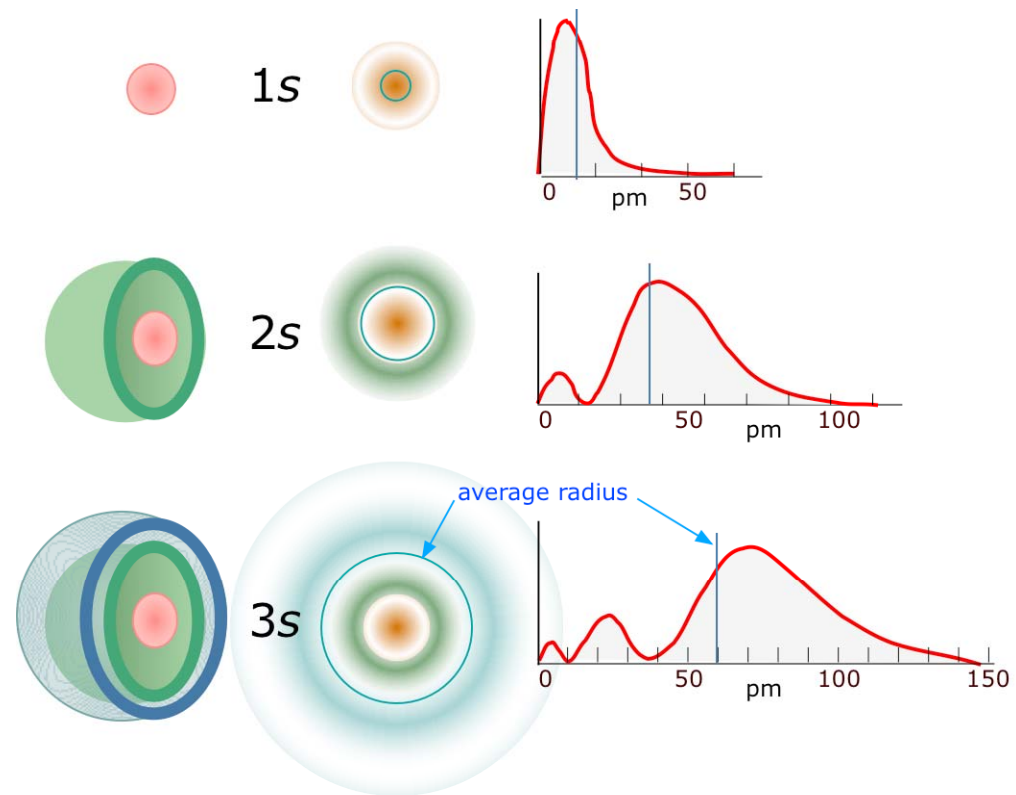
VI. Átomo de hidrogénio

Mecânica quântica - Orbitais atômicos



VI. Átomo de hidrogénio

Mecânica quântica - Orbitais atômicos



VII. Oscilador harmônico quântico

Orbitais quânticos

